

# Evolution equations for vacuum $G_2$ –models containing both Gowdy and Bianchi $VI_{-\frac{1}{9}}^*$

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$$\partial_0 E = (q + 2\Sigma_+)E \quad (1)$$

$$\partial_0 \Sigma_+ = (q - 2)\Sigma_+ - 2(N_-^2 + N_c^2) + \frac{1}{3}(E\partial_x - r)A + 3\Sigma_2^2 - \frac{1}{3}(E\partial_x - r + u + A)u \quad (2)$$

$$\partial_0 \Sigma_- = (q - 2)\Sigma_- - 2\sqrt{3}N_-^2 - (E\partial_x - r + u - 2A)N_c - \sqrt{3}\Sigma_2^2 + 2\sqrt{3}\Sigma_c^2 \quad (3)$$

$$\partial_0 \Sigma_c = (q - 2)\Sigma_c - 2\sqrt{3}N_-N_c + (E\partial_x - r + u - 2A)N_- - 2\sqrt{3}\Sigma_- \Sigma_c \quad (4)$$

$$\partial_0 \Sigma_2 = (q - 2 - 3\Sigma_+ + \sqrt{3}\Sigma_-)\Sigma_2 \quad (5)$$

$$\partial_0 N_- = (q + 2\Sigma_+ + 2\sqrt{3}\Sigma_-)N_- + (E\partial_x - r + u + 2\sqrt{3}N_c)\Sigma_c \quad (6)$$

$$\partial_0 N_c = (q + 2\Sigma_+)N_c - (E\partial_x - r + u)\Sigma_- \quad (7)$$

$$\partial_0 A = (q + 2\Sigma_+)A - (E\partial_x - r - u)(1 + \Sigma_+) \quad (8)$$

Note:

- $q = 2(\Sigma_+^2 + \Sigma_-^2 + \Sigma_2^2 + \Sigma_c^2) + \frac{1}{2}(3\gamma - 2)\Omega - \frac{1}{3}(E\partial_x - r + u - 2A)u$
- $X = (E, \Sigma_+, \Sigma_-, \Sigma_c, \Sigma_2, N_-, N_c, A)$  are functions of  $(x, t)$  where  $x \in S^1$
- $r, u$  are abbreviations composed of variables in the state space  $X$ , like  $q$
- additionally: Equation for Matter (including the “Matter density”  $\Omega$ ), the Gauss and Codazzi constraints...
- $BVI_{-\frac{1}{9}}^*$  is defined by the conditions  $E = u = r = 0$  and  $N_c = \sqrt{3}A$
- Gowdy is defined by  $\Sigma_2 = 0$  and  $A = 0$